1. Suppose $X, Y$ have a bivariate normal distribution with $X \sim \mathcal{N}(0, 1)$ and $Y|X = x \sim \mathcal{N}(ax + b, \sigma^2)$.
   a. What is the marginal distribution of $Y$?
   b. What is the conditional distribution of $X|Y = y$?