Homework for MATH 31A (due Tuesday, 13 October 2009)

*. Use the formulae

$$\frac{\mathrm{d}}{\mathrm{d}x}(x) = 1$$
 and $\frac{\mathrm{d}}{\mathrm{d}x}(fg) = f\frac{\mathrm{d}}{\mathrm{d}x}g + g\frac{\mathrm{d}}{\mathrm{d}x}f$

to prove by mathematical induction that for all $n \in \mathbb{N}$,

$$\frac{\mathrm{d}}{\mathrm{d}x}(x^n) = nx^{n-1}.$$