

## Chef Euclid dmeyer@math.ucsd.edu

Chef Euclid bakes rectangular cakes, but he has only square baking pans. He always uses as few baking pans as possible to bake his cakes, and he never cuts a piece to make it fit.\*

1. Chef Euclid wants to bake a cake that is a  $4in \times 8in$  rectangle. Draw the baking pans he uses. What size, and how many, baking pans does he use?

- 2. What is the greatest number that divides both 4 and 8 evenly?
- 3. Next Chef Euclid wants to bake a cake that is a  $4in \times 10in$  rectangle. Draw the baking pans he uses. What size, and how many, baking pans does he use?



4. What is the greatest number that divides both 4 and 10 evenly?



<sup>\*</sup> See J. Pommersheim, T. Marks and E. Flapan, Number Theory: A Lively Introduction with Proofs, Applications, and Stories (John Wiley & Sons, Inc. 2010).

5. Now Chef Euclid wants to bake a big cake that is a  $18in \times 66in$  rectangle. Draw the baking pans he uses. What size, and how many, baking pans does he use?

- 6. What is the greatest number that divides both 18 and 66 evenly?
- 7. What is the remainder when you divide 252 by 105?
- 8. What is the remainder when you divide 105 by your answer to problem 7?
- 9. What is the remainder when you divide your answer to problem 7 by your answer to problem 8?
- 10. Finally Chef Euclid wants to bake a really big cake that is a  $105in \times 252in$  rectangle. Draw the baking pans he uses. What size, and how many, baking pans does he use?

