Math 20E

August 28, 2012

Question 1 Given a simple domain D with C^1 boundary ∂D, the area of D is given by

A. $A(D) = \iint_D dx\,dy$

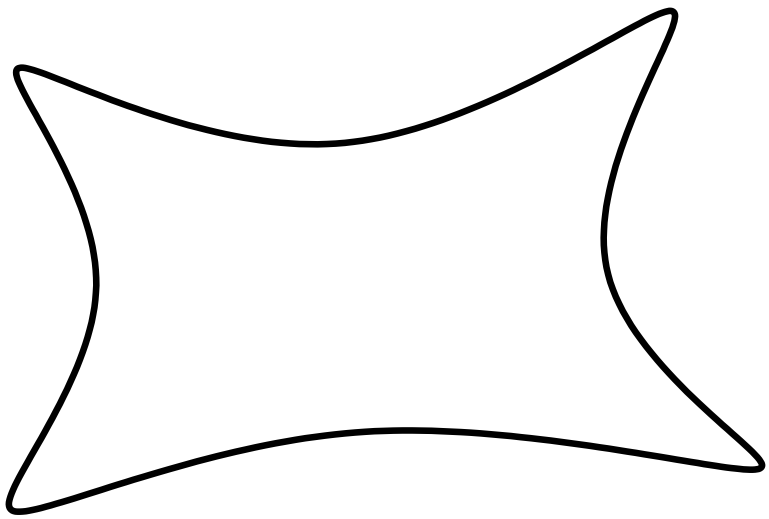
B. $A(D) = -\int_{\partial D} y\,dx$

C. $A(D) = \frac{1}{2}\int_{\partial D} x\,dy - y\,dx$

D. **A** and **C**

*__E.__ **A**, **B** and **C**

Question 2 Consider the following domain D:



A. By Green's theorem, the area of D may be computed by evaluating $\frac{1}{2}\int_{\partial D} x\,dy - y\,dx$.

B. Green's theorem cannot be applied on D since D is not a simple region.

C. The area of D could be measured by tracing ∂D with a planimeter.

***D.** **A** and **C**

E. **B** and **C**

Question 3 Given a C^1 surface S parameterized by $\Phi : D \to S$, and given $\mathbf{F}(x, y, z)$ a continuous vector field defined on S. Then,

A. $\iint_S \mathbf{F} \cdot d\mathbf{S} = \iint_S \mathbf{F} \cdot \mathbf{n}\, dS$, where $\mathbf{n}$ is the unit normal vector at each point of S.

B. The unit normal vector $\mathbf{n}$ at each point of the parametrized surface Φ is given by $\mathbf{n} = \dfrac{\mathbf{T}_u \times \mathbf{T}_v}{||\mathbf{T}_u \times \mathbf{T}_v||}$

C. The average value of the normal component of $\mathbf{F}$ on S is $\dfrac{1}{A(S)} \iint_S \mathbf{F} \cdot d\mathbf{S}$, where $A(S)$ is the area of the surface S.

D. **A** and **B**

***E.** **A**, **B** and **C**